

Breaking tables apart and  
putting them back together

Remy Wang, 4/3/2025

| <b>name</b> | <b>age</b> | <b>bday</b> | <b>kind</b> |
|-------------|------------|-------------|-------------|
| casa        | 8          | 2017-01-01  | cat         |
| kira        | 6          | 2019-09-16  | cat         |
| toby        | 17         | 2008-02-03  | dog         |
| maya        | 10         | 2015-11-21  | dog         |



| <b>name</b> | <b>age</b> | <b>bday</b> | <b>kind</b> |
|-------------|------------|-------------|-------------|
| casa        | 8          | 2017-01-01  | cat         |
| kira        | 6          | 2019-09-16  | cat         |
| maya        | 10         | 2015-11-21  | dog         |



| <b>age</b> | <b>kind</b> |
|------------|-------------|
| 49         | cat         |
| 70         | dog         |

```

SELECT kind, avg(age*7)
FROM pets
WHERE year(bday)>2010;
GROUP BY kind
    
```

## people

### pets

| <b>name</b> | <b>breed</b>     | <b>age</b> | <b>origin</b> | <b>kind</b> |
|-------------|------------------|------------|---------------|-------------|
| casa        | tabby            | 8          | seatte        | cat         |
| kira        | tuxedo           | 6          | hawaii        | cat         |
| toby        | border<br>collie | 17         | seattle       | dog         |
| maya        | husky            | 10         | LA            | dog         |

| <b>name</b> | <b>pet</b> | <b>addr.</b> | <b>phone</b> | <b>job</b> |
|-------------|------------|--------------|--------------|------------|
| remy        | casa       | LA           | ###          | UCLA       |
|             |            |              |              |            |
|             |            |              |              |            |
|             |            |              |              |            |

### places

| <b>name</b> | <b>addr.</b> | <b>type</b> |
|-------------|--------------|-------------|
| UCLA        | LA           | edu.        |
|             |              |             |
|             |              |             |
|             |              |             |

# everything

# everything

# everything

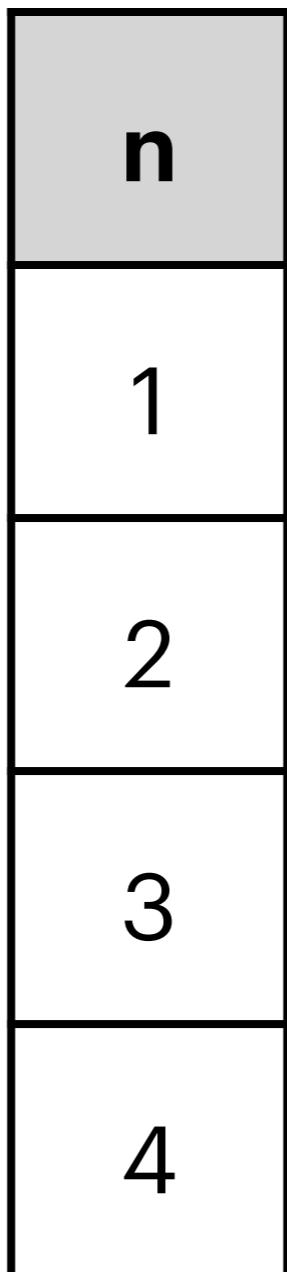
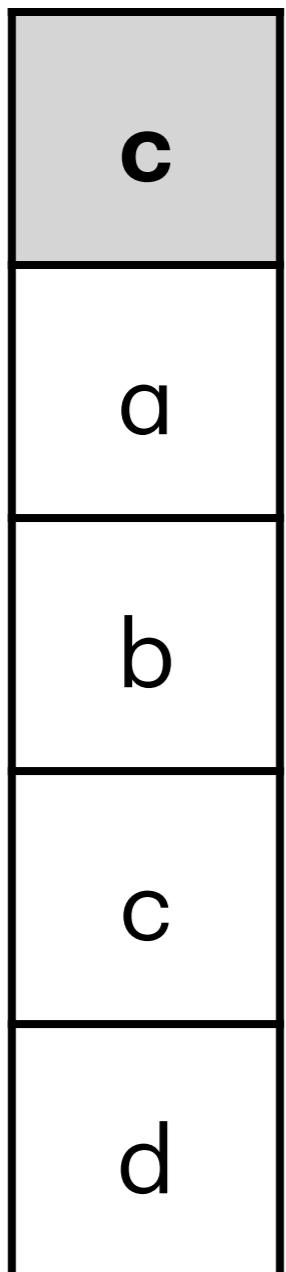
# **everything**

| <b>pet</b> | <b>breed</b>  | <b>age</b> | <b>origin</b> | <b>kind</b> | <b>person</b> | <b>addr.</b> | <b>phone</b> | <b>job</b> |
|------------|---------------|------------|---------------|-------------|---------------|--------------|--------------|------------|
| casa       | tabby         | 8          | seattle       | cat         | remy          | LA           | ###          | UCLA       |
| kira       | tuxedo        | 6          | hawaii        | cat         | remy          | LA           | ###          | UCLA       |
| toby       | border collie | 17         | seattle       | dog         | remy          | LA           | ###          | UCLA       |
| maya       | husky         | 10         | LA            | dog         | remy          | LA           | ###          | UCLA       |
| casa       | tabby         | 8          | seattle       | cat         | remy          | seattle      | ###          | UW         |
| kira       | tuxedo        | 6          | hawaii        | cat         | remy          | seattle      | ###          | UW         |
| toby       | border collie | 17         | seattle       | dog         | remy          | seattle      | ###          | UW         |
| maya       | husky         | 10         | LA            | dog         | remy          | seattle      | ###          | UW         |

Problem: job **independent** from pet!

But what does that mean?

(a detour to probabilities)



$$P(n = 1) =$$

$$P(c = a) =$$

$$P(n = 1 \wedge c = a) =$$

$$P(n = 1 \mid c = a) =$$

$$P(A \mid B) = P(A)$$

A independent from B

$$P(AB) = P(A)P(B) \quad A \perp B$$

# **everything**

| <b>pet</b> | <b>breed</b>  | <b>age</b> | <b>origin</b> | <b>kind</b> | <b>person</b> | <b>addr.</b> | <b>phone</b> | <b>job</b> |
|------------|---------------|------------|---------------|-------------|---------------|--------------|--------------|------------|
| casa       | tabby         | 8          | seattle       | cat         | remy          | LA           | ###          | UCLA       |
| kira       | tuxedo        | 6          | hawaii        | cat         | remy          | LA           | ###          | UCLA       |
| toby       | border collie | 17         | seattle       | dog         | remy          | LA           | ###          | UCLA       |
| maya       | husky         | 10         | LA            | dog         | remy          | LA           | ###          | UCLA       |
| casa       | tabby         | 8          | seattle       | cat         | remy          | seattle      | ###          | UW         |
| kira       | tuxedo        | 6          | hawaii        | cat         | remy          | seattle      | ###          | UW         |
| toby       | border collie | 17         | seattle       | dog         | remy          | seattle      | ###          | UW         |
| maya       | husky         | 10         | LA            | dog         | remy          | seattle      | ###          | UW         |

# **everything**

$$P(\text{kind} = \text{cat}) =$$

$$P(\text{job} = \text{UCLA}) =$$

$$P(\text{cat} \wedge \text{UCLA}) =$$

$\text{kind} \perp \text{job}$

| kind |
|------|
| cat  |
| cat  |
| dog  |
| dog  |
| cat  |
| cat  |
| dog  |
| dog  |

| job  |
|------|
| UCLA |
| UW   |
| UW   |
| UW   |
| UW   |

| <b>kind</b> | <b>person</b> | <b>job</b> |
|-------------|---------------|------------|
| cat         | remy          | UCLA       |
| dog         | remy          | UCLA       |
| cat         | remy          | UW         |
| dog         | remy          | UW         |
| cat         | vincent       | UCLA       |

$$P(\text{cat}) =$$

$$P(\text{cat} \mid \text{UCLA}) =$$

Not independent!

| kind | person  | job  |
|------|---------|------|
| cat  | remy    | UCLA |
| dog  | remy    | UCLA |
| cat  | remy    | UW   |
| dog  | remy    | UW   |
| cat  | vincent | UCLA |

Break down by **person**

$$P(\text{cat}) = P(\text{cat} \mid \text{UCLA}) =$$

kind  $\perp$  job  $\mid$  person

$$P(\text{cat}) = P(\text{cat} \mid \text{UCLA}) =$$

| kind | person  | job  |
|------|---------|------|
| cat  | remy    | UCLA |
| dog  | remy    | UCLA |
| cat  | remy    | UW   |
| dog  | remy    | UW   |
| cat  | vincent | UCLA |

no probabilities? no prob

kind = cat, job = { } }

kind = dog, job = { } }

check for each **person**:

every kind has same set of jobs?

| kind | person  | job  |
|------|---------|------|
| cat  | remy    | UCLA |
| dog  | remy    | UCLA |
| cat  | remy    | UW   |
| dog  | remy    | UW   |
| cat  | vincent | UCLA |

$\#\{ \cdot \} = \text{COUNT DISTINCT}$

$\#\{(k, j)\} = \#\{k\} * \#\{j\}$

$$\frac{1}{P(KJ)} = \frac{1}{P(K)} \frac{1}{P(J)}$$

$K \perp J$

Dependence is bad,  
now what?

| <b>pet</b> | <b>breed</b>  | <b>age</b> | <b>origin</b> | <b>kind</b> | <b>person</b> | <b>addr.</b> | <b>phone</b> | <b>job</b> |
|------------|---------------|------------|---------------|-------------|---------------|--------------|--------------|------------|
| casa       | tabby         | 8          | seattle       | cat         | remy          | LA           | ###          | UCLA       |
| kira       | tuxedo        | 6          | hawaii        | cat         | remy          | LA           | ###          | UCLA       |
| toby       | border collie | 17         | seattle       | dog         | remy          | LA           | ###          | UCLA       |
| maya       | husky         | 10         | LA            | dog         | remy          | LA           | ###          | UCLA       |
| casa       | tabby         | 8          | seattle       | cat         | remy          | seattle      | ###          | UW         |
| kira       | tuxedo        | 6          | hawaii        | cat         | remy          | seattle      | ###          | UW         |
| toby       | border collie | 17         | seattle       | dog         | remy          | seattle      | ###          | UW         |
| maya       | husky         | 10         | LA            | dog         | remy          | seattle      | ###          | UW         |

| pet  | breed         | age | origin  | kind | person | addr.   | phone | job  |
|------|---------------|-----|---------|------|--------|---------|-------|------|
| casa | tabby         | 8   | seattle | cat  | remy   | LA      | ###   | UCLA |
| kira | tuxedo        | 6   | hawaii  | cat  | remy   | LA      | ###   | UCLA |
| toby | border collie | 17  | seattle | dog  | remy   | LA      | ###   | UCLA |
| maya | husky         | 10  | LA      | dog  | remy   | LA      | ###   | UCLA |
| casa | tabby         | 8   | seattle | cat  | remy   | seattle | ###   | UW   |
| kira | tuxedo        | 6   | hawaii  | cat  | remy   | seattle | ###   | UW   |
| toby | border collie | 17  | seattle | dog  | remy   | seattle | ###   | UW   |
| maya | husky         | 10  | LA      | dog  | remy   | seattle | ###   | UW   |

**SELECT DISTINCT ... , person  
FROM everything**

**How?      SELECT DISTINCT ...  
                FROM everything**

| pet  | breed         | age | origin  | kind | person |
|------|---------------|-----|---------|------|--------|
| casa | tabby         | 8   | seattle | cat  | remy   |
| kira | tuxedo        | 6   | hawaii  | cat  | remy   |
| toby | border collie | 17  | seattle | dog  | remy   |
| maya | husky         | 10  | LA      | dog  | remy   |

| person | addr.   | phone | job  |
|--------|---------|-------|------|
| remy   | LA      | ###   | UCLA |
| remy   | seattle | ###   | UW   |

| person  | addr. | phone | job  | job addr. |
|---------|-------|-------|------|-----------|
| remy    | ...   | 123   | UCLA | LA        |
| zifan   | ...   | 234   | UCLA | LA        |
| vincent | ...   | 345   | UCLA | LA        |
| remy    | ...   | 123   | UW   | seattle   |
| dan     | ...   | 456   | UW   | seattle   |
| magda   | ...   | 567   | UW   | seattle   |

job **determines** job addr.

$$P(\text{LA} \mid \text{UCLA}) = 1$$

| <b>person</b> | <b>addr.</b> | <b>phone</b> | <b>job</b> |
|---------------|--------------|--------------|------------|
| remy          | ...          | 123          | UCLA       |
| zifan         | ...          | 234          | UCLA       |
| vincent       | ...          | 345          | UCLA       |
| remy          | ...          | 123          | UW         |
| dan           | ...          | 456          | UW         |
| magda         | ...          | 567          | UW         |

| <b>job</b> | <b>job addr.</b> |
|------------|------------------|
| UCLA       | LA               |
| UW         | seattle          |

| person  | addr. | phone | job  |
|---------|-------|-------|------|
| remy    | ...   | 123   | UCLA |
| zifan   | ...   | 234   | UCLA |
| vincent | ...   | 345   | UCLA |
| remy    | ...   | 123   | UW   |
| dan     | ...   | 456   | UW   |
| magda   | ...   | 567   | UW   |

| job  | job addr. |
|------|-----------|
| UCLA | LA        |
| UW   | seattle   |

Where's Remy's office?

| <b>pet</b> | <b>breed</b>  | <b>age</b> | <b>origin</b> | <b>kind</b> | <b>person</b> |
|------------|---------------|------------|---------------|-------------|---------------|
| casa       | tabby         | 8          | seattle       | cat         | remy          |
| kira       | tuxedo        | 6          | hawaii        | cat         | remy          |
| toby       | border collie | 17         | seattle       | dog         | remy          |
| maya       | husky         | 10         | LA            | dog         | remy          |

| <b>name</b> | <b>addr.</b> | <b>phone</b> | <b>job</b> |
|-------------|--------------|--------------|------------|
| remy        | LA           | ###          | UCLA       |
| remy        | seattle      | ###          | UW         |

Where do cat people work?

| pet  | breed         | age | origin  | kind | person | addr.   | phone | job  |
|------|---------------|-----|---------|------|--------|---------|-------|------|
| casa | tabby         | 8   | seattle | cat  | remy   | LA      | ###   | UCLA |
| kira | tuxedo        | 6   | hawaii  | cat  | remy   | LA      | ###   | UCLA |
| toby | border collie | 17  | seattle | dog  | remy   | LA      | ###   | UCLA |
| maya | husky         | 10  | LA      | dog  | remy   | LA      | ###   | UCLA |
| casa | tabby         | 8   | seattle | cat  | remy   | seattle | ###   | UW   |
| kira | tuxedo        | 6   | hawaii  | cat  | remy   | seattle | ###   | UW   |
| toby | border collie | 17  | seattle | dog  | remy   | seattle | ###   | UW   |
| maya | husky         | 10  | LA      | dog  | remy   | seattle | ###   | UW   |

JOIN



| name | addr.   | phone | job  |
|------|---------|-------|------|
| remy | LA      | ###   | UCLA |
| remy | seattle | ###   | UW   |

| pet  | breed         | age | origin  | kind | person |
|------|---------------|-----|---------|------|--------|
| casa | tabby         | 8   | seattle | cat  | remy   |
| kira | tuxedo        | 6   | hawaii  | cat  | remy   |
| toby | border collie | 17  | seattle | dog  | remy   |
| maya | husky         | 10  | LA      | dog  | remy   |

```
SELECT job FROM
pets JOIN people
ON pets.person = people.name
```

Join key

| pet  | breed         | age | origin  | kind | person |
|------|---------------|-----|---------|------|--------|
| casa | tabby         | 8   | seattle | cat  | remy   |
| kira | tuxedo        | 6   | hawaii  | cat  | remy   |
| toby | border collie | 17  | seattle | dog  | remy   |
| maya | husky         | 10  | LA      | dog  | remy   |

| name | addr.   | phone | job  |
|------|---------|-------|------|
| remy | LA      | ###   | UCLA |
| remy | seattle | ###   | UW   |

```

for pet in pets:
    for person in people:
        if pet.person = person.name:
            print(job)

```

## Join key

| <b>pet</b> | <b>breed</b>     | <b>age</b> | <b>origin</b> | <b>kind</b> | <b>person</b> |
|------------|------------------|------------|---------------|-------------|---------------|
| casa       | tabby            | 8          | seattle       | cat         | remy          |
| kira       | tuxedo           | 6          | hawaii        | cat         | remy          |
| toby       | border<br>collie | 17         | seattle       | dog         | remy          |
| maya       | husky            | 10         | LA            | dog         | remy          |

| <b>name</b> | <b>addr.</b> | <b>phone</b> | <b>job</b> |
|-------------|--------------|--------------|------------|
| remy        | LA           | ###          | UCLA       |
| remy        | seattle      | ###          | UW         |

```

for pet in pets:
    for person in people:
        print(job)
    
```

Join key

| <b>pet</b> | <b>breed</b>     | <b>age</b> | <b>origin</b> | <b>kind</b> | <b>person</b> |
|------------|------------------|------------|---------------|-------------|---------------|
| casa       | tabby            | 8          | seattle       | cat         | remy          |
| kira       | tuxedo           | 6          | hawaii        | cat         | remy          |
| toby       | border<br>collie | 17         | seattle       | dog         | remy          |
| maya       | husky            | 10         | LA            | dog         | remy          |

| <b>name</b> | <b>addr.</b> | <b>phone</b> | <b>job</b> |
|-------------|--------------|--------------|------------|
| remy        | LA           | ###          | UCLA       |
| remy        | seattle      | ###          | UW         |

$$T_1\bowtie_p T_2=\sigma_p(T_1\times T_2)$$

```
SELECT job FROM  
pets JOIN people  
ON pets.person = people.name
```

```
SELECT job  
FROM pets, people  
WHERE pets.person = people.name
```

$job \in \text{output}$



$\exists a \in \text{pets}, p \in \text{people} : p.job = job$   
 $\wedge a.person = p.name$

**SELECT R.x, AVG(T.z)**

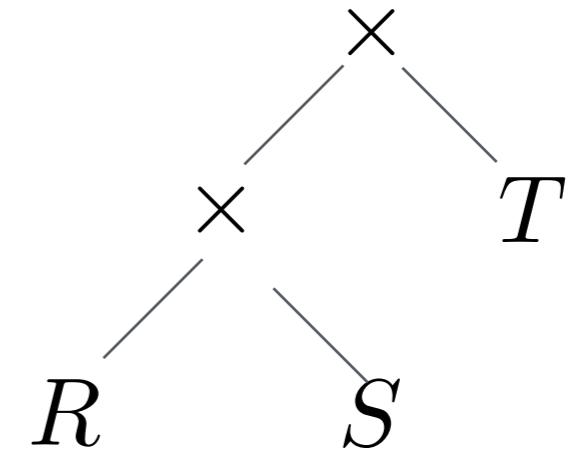
**FROM R, S, T**

**WHERE R.x = S.x  
AND S.y = T.y**

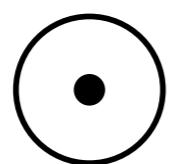
**GROUP BY R.x**

$\gamma_{x,\text{avg}}(z)$

$\sigma_{R.x=S.x \wedge S.y=T.y}$



|   |
|---|
| i |
| 1 |
| 2 |
| 3 |
| 4 |
| 5 |
| 6 |



|   |
|---|
| i |
| 1 |
| 2 |
| 3 |
| 4 |
| 5 |
| 6 |

|    |
|----|
| i  |
| 1  |
| 4  |
| 9  |
| 16 |
| 25 |
| 36 |

|   |
|---|
| i |
| 1 |
| 2 |
| 3 |
| 4 |
| 5 |
| 6 |

×

|   |
|---|
| i |
| 1 |
| 2 |
| 3 |
| 4 |
| 5 |
| 6 |

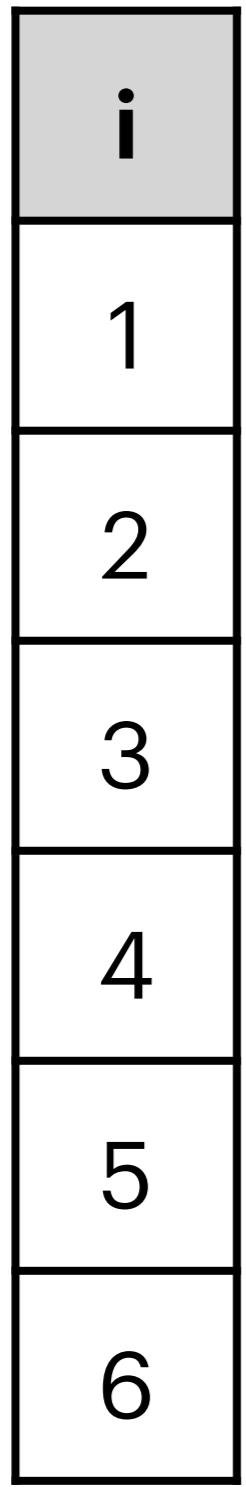
|  |  |  |  |  |
|--|--|--|--|--|
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |

X

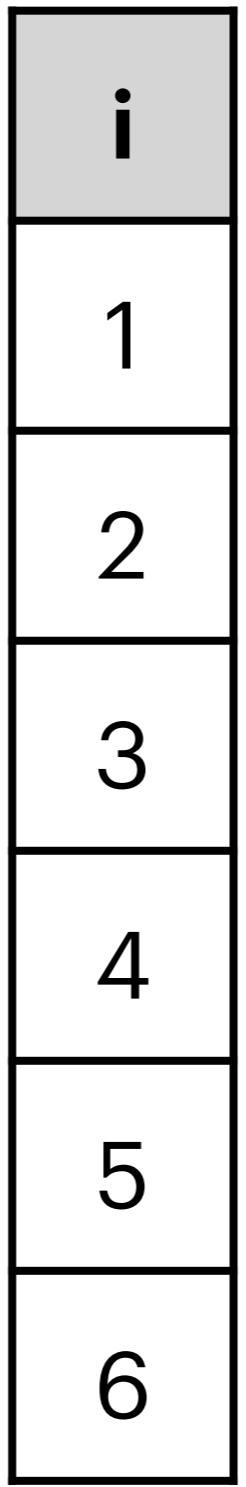
|   |   |   |   |   |   |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
|---|---|---|---|---|---|

- 1
- 2
- 3
- 4
- 5
- 6

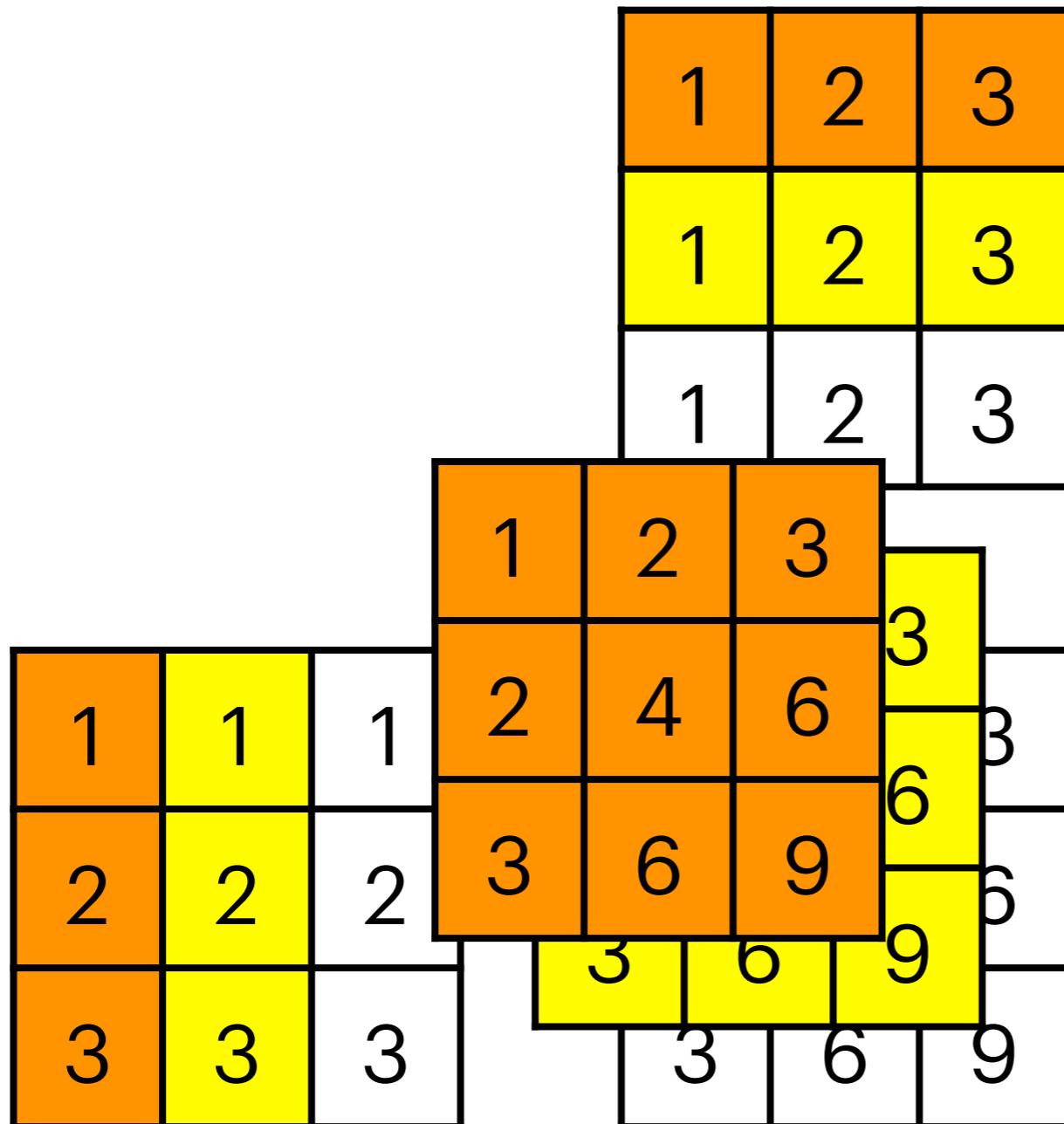
A 6x6 grid of empty cells, represented by a black border around a white area divided into six columns and six rows by black lines.



•



$$u \cdot v = \sum u \odot v$$



$$AB_{ik} = \sum_j A_{ij} \times B_{jk}$$

$f$ 

| I | O |
|---|---|
| 1 | 2 |
| 2 | 3 |
| 3 | 4 |
| 4 | 5 |

 $g$ 

| I | O  |
|---|----|
| 2 | 4  |
| 3 | 6  |
| 4 | 8  |
| 5 | 10 |

$$g \circ f(x) = g(f(x))$$

| I | O  |
|---|----|
| 1 | 4  |
| 2 | 6  |
| 3 | 8  |
| 4 | 10 |